

Inverse Rendering with Spherical Gaussians for Physics-based Material Editing and Relighting Supplemental Document

In this supplemental document, we first provide details of the specular BRDF model used in our pipeline. Then, additional results on the synthetic data are included. Finally, we show additional results with videos.

1. Specular BRDF

Suppose the specular albedo is $s \in [0, 1]^3$ and roughness is $R \in \mathcal{R}_+$. We use the following simplified Disney BRDF model for specular BRDF $f_s(\omega_o, \omega_i)$ as in prior works [1, 3]:

$$f_s(\omega_o, \omega_i) = \mathcal{M}(\omega_o, \omega_i)\mathcal{D}(\mathbf{h}), \tag{1}$$

$$\mathbf{h} = \frac{\omega_o + \omega_i}{\|\omega_o + \omega_i\|_2}, \tag{2}$$

$$\mathcal{M}(\omega_o, \omega_i) = \frac{\mathcal{F}(\omega_o, \omega_i)\mathcal{G}(\omega_o, \omega_i)}{4(\mathbf{n} \cdot \omega_o)(\mathbf{n} \cdot \omega_i)}, \tag{3}$$

$$\mathcal{F}(\omega_o, \omega_i) = s + (1 - s) \cdot 2^{-(5.55473\omega_o \cdot \mathbf{h} + 6.8316)(\omega_o \cdot \mathbf{h})}, \tag{4}$$

$$\mathcal{G}(\omega_o, \omega_i) = \frac{\omega_o \cdot \mathbf{n}}{\omega_o \cdot \mathbf{n}(1 - k) + k} \cdot \frac{\omega_i \cdot \mathbf{n}}{\omega_i \cdot \mathbf{n}(1 - k) + k}, \tag{5}$$

$$k = \frac{(R + 1)^2}{8}, \tag{6}$$

$$\mathcal{D}(\mathbf{h}) = G(\mathbf{h}; \mathbf{n}, \frac{2}{R^4}, \frac{1}{\pi R^4}), \tag{7}$$

where \mathcal{F}, \mathcal{G} are Fresnel and shadowing terms, respectively, and \mathcal{D} is the normalized distribution function.

2. Additional synthetic examples



Figure 1: Results of our pipeline on synthetic data. For a novel test view, we compare our predicted image, estimated diffuse albedo, specular BRDF editing results and relighting results against the ground-truth rendered by Mitsuba [2].

3. Video demos

Please qualitatively inspect our results demonstrated in the supplemental video (included in the zip file) on the real-world SLF fish [6], DeepVoxels coffee [5], and Chips cans [4] datasets.

References

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